

$$\int \cos^2 x \, dx =$$

INT-S1-049

PER PARTI

$$= \int \cos x \cdot \cos x \, dx = [\int \cos x] \cos x - \int [\int \cos x] [D \cos x] \, dx =$$

$$= +\sin x \cos x - \int \sin x (\sin x) \, dx =$$

$$= \sin x \cos x + \int \sin^2 x \, dx =$$

$$= \sin x \cos x + \int 1 - \cos^2 x \, dx =$$

$$= \sin x \cos x + \int 1 \, dx - \int \cos^2 x \, dx =$$

$$= \sin x \cos x + x - \int \cos^2 x \, dx$$

QUINDI ABBIAMO :

$$\int \cos^2 x \, dx = \sin x \cos x + x - \int \cos^2 x \, dx \rightarrow$$

$$\rightarrow \int \cos^2 x \, dx + \int \cos^2 x \, dx = \sin x \cos x + x \rightarrow$$

$$\rightarrow 2 \int \cos^2 x \, dx = \sin x \cos x + x$$

$$\rightarrow \int \cos^2 x \, dx = \boxed{\frac{1}{2} \sin x \cos x + \frac{1}{2} x + k}$$

$$\text{ALTRO MODO: } \int \cos^2 x \, dx = \frac{1}{2} \int (2 \cos^2 x - 1 + 1) \, dx = \frac{1}{2} \int (\cos 2x + \frac{1}{2}) \, dx =$$
$$= \frac{1}{4} \sin 2x + \frac{1}{2} x + k = \frac{1}{2} \sin x \cos x + \frac{1}{2} x + k$$